

Observation of $\Delta|k - l| = 3$ Transitions in the ν_3 Band of H_3O^+

D. Uy,¹ E. T. White, and T. Oka

Department of Chemistry and Department of Astronomy and Astrophysics, The University of Chicago, Chicago, Illinois 60637

Received August 12, 1996; in revised form January 13, 1997

Although the vibration–rotation spectrum of H_3O^+ has been studied extensively, there has been no experimental information on the value of the C rotational constant because of the absence of any observed $\Delta|k - l| \neq 0$ forbidden transitions. However, as pointed out by Verhoeve *et al.* in their far-infrared spectroscopic work [P. Verhoeve, M. Versluis, J. J. Ter Meulen, W. L. Meerts, and A. Dynamus, *Chem. Phys. Lett.* **161**, 195–201 (1989)], a near degeneracy exists between some $(J, 0)^+$ and $(J, 3)^-$ ground state rotation–inversion levels, which causes sizable shifts in these levels due to off-diagonal centrifugal distortion. These shifts were observed in the ground state combination differences of the ν_3 fundamental transitions. We have observed 11 forbidden $\Delta|k - l| = 3$ transitions to the ν_3 band induced by the mixing in the ground state and involving the $J = 7, 9$, and 11 levels, and determined the energy difference between different K levels, the C rotational constant, and the off-diagonal centrifugal distortion mixing coefficient. © 1997 Academic Press

INTRODUCTION

Over the past decade, the vibration–inversion–rotation spectrum of the H_3O^+ ion has been investigated by experimentalists and theoreticians since its first high-resolution gas phase spectrum in the $3 \mu\text{m}$ region was reported in 1983 (1). It is a fundamental molecular ion crucial in many biochemical and organic reactions and in the ion-molecule reaction scheme in dense interstellar clouds (2). H_3O^+ is structurally and dynamically similar to its isoelectronic species NH_3 with its pyramidal structure and rotation–vibration levels split by inversion. In the ground vibrational state, it has a large inversion splitting of 55.34 cm^{-1} (3, 4). Since this value happens to be close to $9(B - C)$, there exists a near degeneracy between the $(J, K = 0)$ levels in the (+) inversion state and the $(J, K = 3)$ levels in the (–) inversion state for odd values of J . The two levels are closest at $J = 9$ and considerable mixing of these levels is expected. The rotation of the molecule perpendicular to the symmetry axis induces a small dipole moment by centrifugal distortion (5), which mixes the $|J, K = 0, 0^+\rangle$ and $|J, K = 3, 0^-\rangle$ levels. Thus, it has been predicted (4, 6, 7) that forbidden $\Delta k = 3$ transitions may be observable in the ν_2 band of H_3O^+ . Similar transitions have been detected due to similar mixing in the ν_2 state of NH_3 (8, 9).

In this article, we report our observation of 11 forbidden $\Delta|k - l| = 3$ transitions in the ν_3 band of H_3O^+ due to $\Delta k = \pm 3$ mixing in the ground state. They were detected following our observation of shifts in the $K = 3$ antisymmetric ground state levels while working on an extended analysis

of the ν_3 band. Although the vibration–rotation spectrum of H_3O^+ has been studied extensively, no $\Delta|k - l| \neq 0$ transitions have been previously assigned and experimental information on the C rotational constant has not been available. The $\Delta|k - l| = 3$ transitions we obtained enabled us to determine the energy difference between the different K levels and thus the values of $C - 9D_{kk}$ and the mixing coefficient.

EXPERIMENTAL

The spectrum of H_3O^+ was obtained using either a difference frequency laser spectrometer (10) or a color center laser spectrometer (11) with the velocity modulation technique (12). In the difference frequency spectrometer, the radiation from a single-mode Ar ion laser and a tunable ring dye laser are combined in a temperature-controlled LiNbO_3 crystal to generate infrared radiation with a frequency of $\nu_{\text{Ar}} - \nu_{\text{dye}}$. With the color center spectrometer, infrared radiation is generated by pumping an $\text{F}_A(\text{II})$ -type $\text{RbCl}:\text{Li}$ crystal by a Kr ion laser, which was tuned by scanning the voltage of a piezoelectrically controlled intracavity étalon while the grating was slowly adjusted. In both systems, 10% of the infrared radiation generated was sent to a reference gas for frequency calibration while the remaining portion of the radiation was directed to a water-cooled ac glow discharge where H_3O^+ was produced. The infrared radiation was divided into two beams of equal power, with each beam traversing the discharge cell three or four times unidirectionally in a modified White cell configuration. It was then sent to two matched InSb detectors where the detected signals were combined in opposite phase in a pair of audio frequency transformers and sent

¹ Present address: JILA, Campus Box 440, University of Colorado at Boulder, Boulder, CO 80309.

to a lock-in amplifier for signal amplification. The signals were simultaneously recorded with a chart recorder and a computer.

The H_3O^+ ions were produced using three different gas mixtures: (a) 100 mT H_2 , 100 mT O_2 , 10 Torr He; (b) 250–450 mT of gas from a 50% H_2O_2 –water solution and 7 Torr He; and (c) 550 mT H_2 and 150 mT O_2 . The discharge was powered by either a Plasmalok RS-8 operating at 25 kHz or an audio amplifier (Tecron 7550) coupled to a step-up transformer at 6 kHz. The voltage and current were about 10 kV and 300 mA with the Plasmalok, and approximately half of these with the audio amplifier and transformer. The glass discharge cells were 1 meter long with inner diameters of 12 and 18 mm and multiple gas inlets and outlets running along their lengths. Wavenumber calibration was provided by spectral lines of NH_3 (13) and H_2O (14). The accuracy of the frequency measurement was 0.01 cm^{-1} for the color center spectrometer and 0.006 cm^{-1} for the difference frequency spectrometer.

EXPERIMENTAL GROUND STATE COMBINATION DIFFERENCES AND $\Delta k = 3$ MIXING

Because of the inversion motion of H_3O^+ with D_{3h} symmetry, its ground vibrational state splits into a symmetric $|0^+\rangle$ level with A_1' symmetry and an antisymmetric $|0^-\rangle$ level with A_2'' symmetry. From nuclear spin statistics and the Pauli principle, only $J = \text{odd}$ levels are allowed for $K = 0$ in the $|0^+\rangle$ state and $J = \text{even}$ levels for the $K = 0$ $|0^-\rangle$ state. Because of the rotational parity of $(-1)^K$ and the selection rule $\Delta K = \pm 1$, the ν_3 –0 transition is

allowed between symmetric–symmetric and antisymmetric–antisymmetric vibration–inversion states, with the usual selection rules of $\Delta J = 0, \pm 1$.

The ν_3 band of H_3O^+ has been previously studied by several workers (1, 11, 15–17). While we were extending the analysis of this band to higher J and K rotational levels, we observed large differences between the experimental and calculated ground state combination differences for the antisymmetric band for $K = 3$ levels (See Table 1). The ground state combination differences were calculated from the usual energy level expression for an oblate symmetric top

$$E(J, K) = BJ(J+1) + (C-B)K^2 - D_{ij}J^2(J+1)^2 - D_{jk}J(J+1)K^2 - D_{kk}K^4 + H_{jjj}J^3(J+1)^3 + H_{jjk}J^2(J+1)^2K^2 + H_{jkk}J(J+1)K^4 + H_{kkk}K^6 \quad [1]$$

using the constants given in Ref. (4) which are derived from the far infrared rotation–inversion spectrum. From the values of the discrepancy between the observed and calculated, it was clear that the odd J levels with $K = 3$ were perturbed by nearby levels while even J levels were unshifted. This reminded us of the work by Verhoeve *et al.* (4) who suggested that the shifts in the $|J = \text{odd}, K = 3, 0^-\rangle$ levels were due to the presence of the $|J = \text{odd}, K = 0, 0^+\rangle$ levels, while the $|J = \text{even}, K = 3, 0^-\rangle$ states were unperturbed because $|J = \text{even}, K = 0, 0^+\rangle$ were nonexistent. These pairs of levels have the same symmetry since the rotational parity of a symmetric top is $(-1)^K$.

TABLE 1
Observed and Calculated Ground State Combination Differences in the $|0^-\rangle$ State, from ${}^oQ(J, 3) - {}^oP(J+1, 3)$ (left column) and ${}^pQ(J, 3) - {}^pP(J+1, 3)$ (right column) in cm^{-1}

$(J+1, 3) - (J, 3)$	Experimental	obs-calc	$(J+1, 3) - (J, 3)$	Experimental	obs-calc
5,3 - 4,3	110.204	-0.006	5,3 - 4,3	110.218	0.008
6,3 - 5,3	131.976	-0.010	6,3 - 5,3	131.988	0.002
7,3 - 6,3	153.658	0.038	7,3 - 6,3	153.663	0.043
8,3 - 7,3	175.050	-0.038	8,3 - 7,3	175.049	-0.039
9,3 - 8,3	196.202	-0.167	9,3 - 8,3	196.192	-0.177
10,3 - 9,3	217.647	0.205	10,3 - 9,3	217.652	0.210
11,3 - 10,3	238.149	-0.137	11,3 - 10,3	238.145	-0.141
12,3 - 11,3	259.012	0.130			

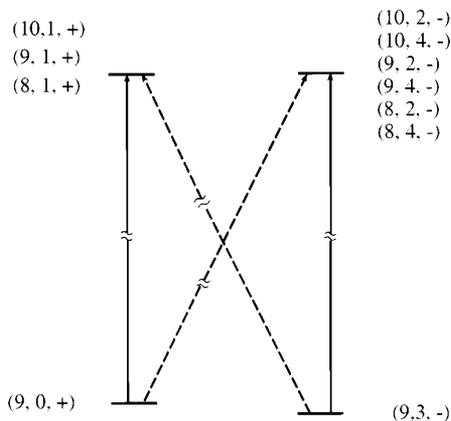


FIG. 1. The allowed and forbidden transitions to the ν_3 band of H_3O^+ due to the mixing of the $(9, 0, 0^+)$ and the $(9, 3, 0^+)$ levels. The solid lines denote the allowed transitions while the broken lines denote the forbidden $\Delta|k-l|=3$ transitions due to the intensity borrowing.

In inverting C_{3v} molecules such as NH_3 and H_3O^+ , there are centrifugal distortion terms that mix states differing by $\Delta k = 3$ (18),

$$H' = \alpha' Q_2 [(J_+^3 + J_-^3) J_z + J_z (J_+^3 + J_-^3)] + i\beta' P_2 (J_+^3 + J_-^3), \quad [2]$$

where α' and β' are the off-diagonal centrifugal distortion constants and $J_{\pm} = J_x \mp iJ_y$. Q_2 and P_2 are the coordinate and momentum, respectively, of the inversion motion. The matrix element connecting the pair of perturbed levels $|J, K = 3, 0^- \rangle$ and $|J, K = 0, 0^+ \rangle$ states is then

$$\langle J, 0, 0^+ | H' | J, 3, 0^- \rangle = \sqrt{2}(3\alpha - \beta) \times [(J+3)!/(J-3)!]^{1/2} \equiv \delta, \quad [3]$$

where $\alpha = \alpha' \langle 0^+ | Q_2 | 0^- \rangle$ and $\beta = -\beta' \langle 0^+ | iP_2 | 0^- \rangle$.

The sizable observed shifts in the ground state energy levels suggest the possibility of observing $\Delta|k-l|=3$ transitions to the ν_3 band, especially for $J=9$, where the energy level shift amounted to 0.2 cm^{-1} . A total of 9 forbidden $\Delta|k-l|=3$ transitions can be observed from the $|J, K = 0, 0^+ \rangle - |J, K = 3, 0^- \rangle$ mixing for each J value (see Fig. 1). Their intensities are weaker by a factor of $(\delta/\Delta E)^2$ compared to the intensities of the allowed transitions, where ΔE is the energy difference between the unperturbed levels that are mixed. Each of the $\Delta|k-l|=3$ transitions would be spaced an equal distance away from the allowed transition, Δ_s , which is the energy difference between the two perturbed levels.

OBSERVED FORBIDDEN TRANSITIONS AND ANALYSIS

Table 2 lists the forbidden $\Delta|k-l|=3$ transitions we have observed for $J=7, 9$, and 11 of the ν_3 band, along

TABLE 2
Observed $\Delta|k-l|=3$ Transitions in H_3O^+ and the Shifts of the Lines (Δ_s) from the Allowed $\Delta|k-l|=0$ Transitions, in cm^{-1}

Allowed	Forbidden	Δ_s	Calculated intensity ratios
${}^1\text{Q}(9,3)^-$ 3469.262	${}^4\text{Q}(9,0)^+$ 3466.750	2.512	1/10
${}^1\text{P}(9,3)^-$ 3275.802	${}^4\text{P}(9,0)^+$ 3273.280	2.522	1/10
${}^{\text{P}}\text{P}(9,3)^-$ 3337.640	${}^{\text{S}}\text{P}(9,0)^+$ 3335.123	2.517	1/10
${}^{\text{P}}\text{Q}(9,3)^-$ 3529.900	${}^{\text{S}}\text{Q}(9,0)^+$ 3527.384	2.516	1/10
${}^{\text{P}}\text{P}(9,0)^+$ 3313.435	${}^{\text{O}}\text{P}(9,3)^-$ 3315.944 ^a	2.509	1/10
${}^{\text{r}}\text{Q}(9,0)^+$ 3513.136	${}^{\text{O}}\text{Q}(9,3)^-$ 3515.651	2.515	1/10
${}^{\text{r}}\text{P}(7,3)^-$ 3323.231	${}^{\text{u}}\text{P}(7,0)^+$ 3325.884	2.653	1/69
${}^{\text{P}}\text{P}(7,3)^-$ 3385.075	${}^{\text{S}}\text{P}(7,0)^+$ 3387.725	2.650	1/69
${}^{\text{P}}\text{Q}(7,3)^-$ 3535.834	${}^{\text{S}}\text{Q}(7,0)^+$ 3538.495	2.661	1/69
${}^{\text{r}}\text{P}(11,3)^-$ 3327.779	${}^{\text{u}}\text{P}(11,0)^+$ 3220.154	7.625	1/37
${}^{\text{P}}\text{P}(11,3)^-$ 3290.155	${}^{\text{S}}\text{P}(11,0)^+$ 3282.529	7.626	1/37

^a This transition is overlapped with another line.

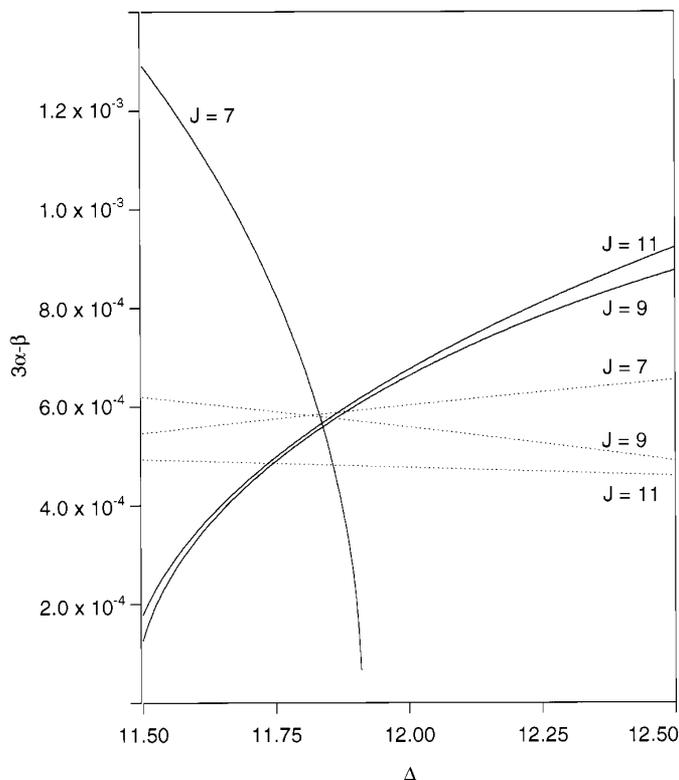


FIG. 2. Plot of Δ (in cm^{-1}) versus $3\alpha - \beta$ (in cm^{-1}) using Eq. [5] for the observed spectral splitting (solid lines) and Eq. [6] for the observed spectral shift (dashed lines) for $J = 7, 9$, and 11 .

with the allowed $\Delta|k - l| = 0$ transitions for each. The superscripts u, s, and o denote $\Delta k = 4, 2, -2$, respectively. We have not obtained any R -branch transitions because of the difficulty of collecting spectral data in these regions due to strong H_2O absorption. Other Q - and P -branch lines not listed in Table 2 were not observed either because of the weakness of the transition or because of the interference of strong water, H_3O^+ , or H_2O^+ absorption.

From the observed $\Delta|k - l| = 3$ transitions resulting from intensity borrowing from allowed transitions, an exper-

imental value for $[C - D_{kk}K^2]$ can now be derived, which is normally undeterminable due to the $\Delta|k - l| = 0$ selection rules of symmetric tops. The mixing coefficient ($3\alpha - \beta$) can also be obtained.

Since the perturbation appreciably mixes only two different levels which are close, their energies can be determined by solving the secular equation

$$\begin{vmatrix} E_0 - \lambda & \delta \\ \delta & E_3 + \Delta - \lambda \end{vmatrix} = 0, \quad [4]$$

where E_0 is the energy of the $|J, K = 0, 0^+\rangle$ state from Eq. [1], and $E_3 + \Delta$ is the energy of the $|J, K = 3, 0^-\rangle$ state where the J independent term $\Delta \equiv [(0^- - 0^+) + 9(C - B) - 81D_{kk}]$ has been separated. This then gives us the solution

$$\Delta_s = \lambda_1 - \lambda_2 = [(E_0 - E_3 - \Delta)^2 + 4\delta^2]^{1/2} \quad [5]$$

and

$$\text{shift} = \frac{1}{2} \Delta_s - \frac{E_0 - (E_3 + \Delta)}{2}, \quad [6]$$

where shift is the difference between the observed and calculated ground state combination differences. Plots of $(3\alpha - \beta)$ versus Δ using Eqs. [5] and [6] for $J = 7, 9$, and 11 are shown in Fig. 2, where the intersection of the lines yield $(3\alpha - \beta) = 5.7 \times 10^{-4} \text{ cm}^{-1}$ and $\Delta = 11.84 \text{ cm}^{-1}$ for H_3O^+ . Equation [5] was also solved numerically using the molecular constants of Ref. (4) for E_0 and E_3 , yielding $(3\alpha - \beta) = 5.7(2) \times 10^{-4} \text{ cm}^{-1}$ and $\Delta = 11.84 \pm 0.02 \text{ cm}^{-1}$.

DISCUSSION AND CONCLUSIONS

Table 3 compares our experimental values for $C''(0^-)$ and $(3\alpha - \beta)$ and those reported in Refs. (4) and (6). We have used the theoretical value of $D_{kk} = 9.267 \times 10^{-4} \text{ cm}^{-1}$

TABLE 3
Determined Constants, in cm^{-1}

	this work	Ref. [4]	Ref. [6]
$C''(0^-)$	6.228(2) ^a	6.42 (6) ^b	6.270
$3\alpha - \beta$	$5.7(2) \times 10^{-4}$	$6.7(10) \times 10^{-4}$	

^aaveraged theoretical value of $D_{kk} = 9.267 \times 10^{-4} \text{ cm}^{-1}$ from Ref. [6] has been used to separate C'' and D_{kk}

^bthe error represents 1σ

TABLE 4
Calculated Shifts of the $|J, 3, 0^- \rangle$ Levels
in cm^{-1}

(J, K)	shift
7, 3	0.036
9, 3	-0.180
11, 3	-0.187

from Ref. (6) to separate C'' and D_{kk} . Our C'' value is different from the previous experimental value beyond the quoted uncertainty, but is closer to the theoretical value (6). Our $(3\alpha - \beta)$ value agrees approximately with that given in Ref. (4). If we use the theoretical value $\alpha = 0.836(200) \times 10^{-4} \text{ cm}^{-1}$ given by Papoušek *et al.* (7), we obtain $\beta = -3.2 \times 10^{-4} \text{ cm}^{-1}$.

Table 4 lists the calculated shifts for $J = 7, 9$, and 11 , which have been obtained using our experimentally determined $(3\alpha - \beta)$. The values agree well with the observed shifts listed in Table 1 for the $J = 7$ and 9 levels. For the $J = 11$ level shift, they differ by 0.046 cm^{-1} , indicating that the energy expression of Eq. [1] is not sufficient for high J levels. We believe that the major cause of this discrepancy is the A_1-A_2 splitting of $K = 3$ levels with the form

$$(-1)^J h_3 (J + 3)! / (J - 3)! \quad [7]$$

The drastic J^6 dependence makes this effect negligible for low J values but significant for $J = 11$. If this interaction is included, we obtain $h_3 = 0.59(12) \times 10^{-10} \text{ cm}^{-1}$. The inclusion of the h_3 term also moves the $J = 11$ shift line closer to the other lines in Fig. 2. However, since our determination of h_3 is dependent effectively on only a few transitions, the value of h_3 may not be accurate.

In conclusion, we have observed 11 $\Delta|k - l| = 3$ transitions in the ν_3 band of H_3O^+ . These transitions have enabled us to obtain values for the C rotational constant for the antisymmetric ground state and an off-diagonal centrifugal distortion constant. A natural extension of this work would

be to find the $\Delta k = 3$ transitions in the far infrared rotation-inversion spectrum and in the ν_2 inversion band. They will appear at positions shifted by the same amount and with the same relative intensities with respect to the allowed transitions as listed in Table 2.

ACKNOWLEDGMENTS

We are grateful to J. K. G. Watson for providing us Eqs. [2] and [3]. We acknowledge the support of the NSF Grant PHYS-9321913.

REFERENCES

1. M. H. Begemann, C. S. Gudeman, J. Pfaff, and R. J. Saykally, *Phys. Rev. Lett.* **51**, 554–557 (1983).
2. T. G. Phillips, E. F. van Dishoeck, and J. Keene, *Astrophys. J.* **399**, 533–550 (1992).
3. D.-J. Liu and T. Oka, *Phys. Rev. Lett.* **54**, 1787–1789 (1985).
4. P. Verhoeve, M. Versluis, J. J. Ter Meulen, W. L. Meerts, and A. Dymanus, *Chem. Phys. Lett.* **161**, 195–201 (1989).
5. T. Oka, in "Molecular Spectroscopy, Modern Research, Vol. II" (K. Narahari Rao, Ed.), pp. 229–253. Academic Press, New York, 1976.
6. V. Špirko and W. P. Kraemer, *J. Mol. Spectrosc.* **134**, 72–81 (1989).
7. D. Papoušek, Š. Urban, V. Špirko, and K. N. Rao, *J. Mol. Struct.* **141**, 361–366 (1986).
8. D. Laughton, S. M. Freund, and T. Oka, *J. Mol. Spectrosc.* **62**, 263–270 (1976).
9. Š. Urban, V. Špirko, D. Papoušek, R. S. McDowell, N. G. Nereson, S. P. Belov, L. I. Gershstein, A. V. Maslovskij, A. F. Krupnov, J. Curtis, and K. Narahari Rao, *J. Mol. Spectrosc.* **79**, 455–495 (1980).
10. M. G. Bawendi, B. D. Rehfuss, and T. Oka, *J. Chem. Phys.* **93**, 6200–6209 (1990).
11. W. C. Ho, C. J. Pursell, and T. Oka, *J. Mol. Spectrosc.* **149**, 530–541 (1991).
12. C. S. Gudeman, M. H. Begemann, J. Pfaff, and R. J. Saykally, *Phys. Rev. Lett.* **50**, 727–731 (1983).
13. J. W. C. Johns, private communication.
14. J. M. Flaud, C. Camy-Peyret, and R. A. Toth, "Selected Constants. Water Vapor Line Parameters from Microwave to Medium IR." Pergamon Press, Oxford, 1981.
15. P. R. Bunker, T. Amano, and V. Špirko, *J. Mol. Spectrosc.* **107**, 208–211 (1984).
16. M. H. Begemann and R. J. Saykally, *J. Chem. Phys.* **82**, 3570–3579 (1985).
17. A. Stahn, H. Solka, H. Adams, and W. Urban, *Mol. Phys.* **60**, 121–128 (1987).
18. S. P. Belov, L. I. Gershstein, A. F. Krupnov, A. V. Maslovskij, Š. Urban, V. Špirko, and D. Papoušek, *J. Mol. Spectrosc.* **84**, 288–304 (1980).